

# CS601: Software Development for Scientific Computing

Autumn 2022

Week13 (3/11/22): Program Representation  
(Grids)

# Program Representation – Structured Grids

- Grid requirements:
  - Grid dimension shall not be hardcoded
    - Consequence: implementations must define a compile-time constant
  - Grid step size shall not be hardcoded E.g.  $h=1/3$ ,  $h=1/5$  etc.
    - Consequence: can't define `int arr[m][n]; //m,n to be constant expr.`
  - A grid point shall be identified with cartesian coordinates / polar coordinates (e.g. with angle and radius from origin)
    - Shall be able to generate a structured grid given number of points,  $\xi$ , and  $\eta$ .
  - Shall allow access to any grid point
  - Shall allow for implementation of grid operators

# Structured Grids - Representation

- Because of regular connectivity between cells
  - Cells can be identified with indices  $(x,y)$  or  $(x,y,z)$  and neighboring cell info can be obtained.
  - How about identifying a cell here?

Given:

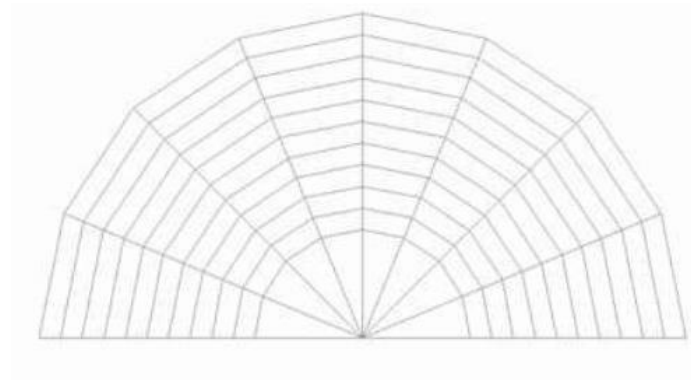
$\xi$  = (“Xi”) radius

$\eta$  = (“Eta”) angle

Compute:

$$x = \left( \frac{1}{2} + \xi \right) \cos(\pi\eta)$$

$$y = \left( \frac{1}{2} + \xi \right) \sin(\pi\eta)$$



# class Domain

- We discretize the domain using a grid

```
class Domain{
    public:
        generate_grid(int m, int n);
        Domain(); // constructor
        //...
    private:
        //...
};
```

# Method GenerateGrid

- What is the shortcoming of the following method?

```
void Domain::GenerateGrid(int m, int n) {
    if (m <=0 || n<=0)
        throw std::invalid_argument("ERR_generate_grid");
    else if( m > 0) {
//there already exists a grid! Attempt to create a grid again
        delete [] x; delete [] y;
    }
    xlen=m;ylen=n; // initialize members
    x=new double[xlen*ylen]; y=new double[xlen*ylen];
}
```

- Assumes a 2D grid.

# Grid Function

- We let a grid function to operate on the grid points
  - Example of an operator: numerical differentiation
  - Different operations possible
  - Note: grid function always operates on some grid.
  - Many functions may operate on the same grid.

```
class GridFn{
    public:
        //...
    private:
        Domain* d; //denotes aggregation relationship
        //...
};
```

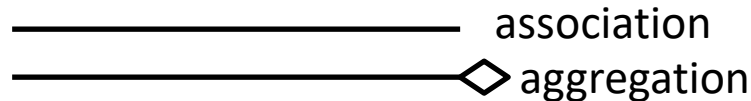
# Detour: Relationships among Classes

- Dependencies (“uses”)

E.g. Customer uses a MS Word editor to produce MS Word document



- Association / Aggregation (“has a”)



E.g. Every course has a name, credits - aggregation  
A student registers for course(s) – association  
between student and course

- Generalization (“is a”)



E.g. Apple is a Fruit (*Apple and Fruit are modeled as classes, where Fruit is a super-class and Apple is a sub-class*)

# Boundary conditions

- Multiple options: affect the accuracy of the solution

Name	Prescription	Interpretation
Dirichlet (essential)	$u$	Fixed temperature
Neumann (Natural)	$\partial u / \partial n$	Energy Flow
Robin (Mixed)	$\partial u / \partial n + f(u)$	Temperature dependent flow

- How to represent boundary conditions?
  - Create a separate Solution class



# Solution

- pseudo-code

```
1 Domain dom; // create domain
2 GridFn g(dom); //create grid function to operate on a domain
3 Solution u(g) //prepare to compute a solution:
4 u.initcond() //1) set initial conditions
5 for(int step=0; step<maxsteps; step++) 2) iterate:
6 {
7     u.compute(); //2) compute solution repeatedly
8 }
```

# class Solution

- We discretize the domain using a grid

```
class Solution{
    public:
        Solution(GridFn* d): sol(d) {}
        initcond();
        boundarycond();
        //... other member functions?
    private:
        GridFn* sol;
};
```

# What is missing?

- Data array?
  - We need to make provision for storing the results of algebraic equations (temperature, displacements, stress, strain etc.)
- Type of data as template parameter?
  - Does the application accept single-precision results?  
Double-precision results?
- Operation on subgrids (Box)?
  - When a particular grid function is applied only in a certain region