

CS406: Compilers

Spring 2021

Week 4: Parsers

Parsing – so far..

- Parsing involves:
 - identifying if a program has *syntax errors*
 - Identifying the *structure* of a valid program
- CFGs are formal notations for specifying the rules of the programming language
 - Has *symbols* (start, terminal(s), non-terminal(s)), and *productions/rules*
 - *Derivations* are a sequence of expansions of a string of symbols
Left-most derivation and *Right-most derivation* are popular methods defining the order in the sequence

Parsing – so far..

- Parse trees are tree structures having terminals as leaves and non-terminals as nodes
 - The sequence involved in derivations define them
 - For a given string having *terminal symbols only*, there exists *only one parse tree* in an *unambiguous grammar*
 - A grammar is ambiguous if there exists some string for which different derivations result in more than one tree structure
- Ambiguity fixing in grammars
 - Manual rewriting of grammar
 - Hints to parser generators
- Error handling in parsers
 - Panic mode, error productions, and error recovery.

Top-down Parsing

- Idea: we know sentence has to start with initial symbol
- Build up partial derivations by *predicting* what rules are used to expand non-terminals
 - Often called *predictive parsers*
- If partial derivation has terminal characters, *match* them from the input stream

Top-down Parsing

- Also called recursive-descent parsing
- Equivalent to finding the left-derivation for an input string
 - Recall: expand the leftmost non-terminal in a parse tree
 - Expand the parse tree in pre-order i.e., identify parent nodes before children

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

Step	Input string	Parse tree
1	cad ↑	S

String: cad

Start with S

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

Step	Input string	Parse tree
1	cad	S
2	↑ cad ↑	<pre>graph TD; S --> c; S --> A; S --> d; A --> a; A --> b;</pre>

String: cad

Predict rule 1

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

String: cad

Predict rule 2

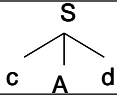
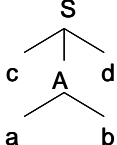
Step	Input string	Parse tree
1	cad	S
2	↑ cad	<pre>graph TD; S --> c; S --> A; S --> d;</pre>
3	cad ↑	<pre>graph TD; S --> c; S --> A; S --> d; A --> a; A --> b;</pre>

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

String: cad

Step	Input string	Parse tree
1	cad	S
2	↑ cad	
3	cad ↑	

No more non terminals!
String doesn't match.
Backtrack.

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

Step	Input string	Parse tree
1	cad	S
2	↑ cad ↑	<pre>graph TD; S1[S] --- c1[c]; S1 --- A1[A]; S1 --- d1[d]; A1 --- a1[a]; A1 --- b1[b];</pre>

String: cad

Top-down Parsing

↑: next symbol to be read

- 1: $S \rightarrow cAd$
- 2: $A \rightarrow ab$
- 3: | a

String: cad

Predict rule 3

Step	Input string	Parse tree
1	cad	S
2	cad ↑	<pre>graph TD; S --> c; S --> A; S --> d; style A stroke:#f00,stroke-width:2px</pre>
4	cad ↑	<pre>graph TD; S --> c; S --> A; S --> d; A --> a; style a stroke:#f00,stroke-width:2px</pre>

Top-down Parsing – Table-driven Approach

- 1: $S \rightarrow F$
- 2: $S \rightarrow (S + F)$
- 3: $F \rightarrow a$

string: (a+a)

string': (a+a)\$

	()	a	+	\$
S	2	-	1	-	-
F	-	-	3	-	-

Assume that the table is given.

- Table-driven (Parse Table) approach doesn't require backtracking

But how do we construct such a table?

Important Concepts: First Sets and Follow Sets

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Concepts for analyzing the grammar

First and follow sets

- $\text{First}(\alpha)$: the set of terminals (and/or λ) that begin all strings that can be derived from α

- $\text{First}(A) = \{x, y, \lambda\}$

- $\text{First}(xA) = \{x\}$

- $\text{First}(AB) = \{x, y, b\}$

- $\text{Follow}(A)$: the set of terminals (and/or $\$,$ but no λ s) that can appear immediately after A in some partial derivation

- $\text{Follow}(A) = \{b\}$

$$S \rightarrow A B \$$$

$$A \rightarrow x a A$$

$$A \rightarrow y a A$$

$$A \rightarrow \lambda$$

$$B \rightarrow b$$

First and follow sets

- $\text{First}(\alpha) = \{a \in V_t \mid \alpha \Rightarrow^* a\beta\} \cup \{\lambda \mid \text{if } \alpha \Rightarrow^* \lambda\}$
- $\text{Follow}(A) = \{a \in V_t \mid S \Rightarrow^+ \dots Aa \dots\} \cup \{\$ \mid \text{if } S \Rightarrow^+ \dots A \$\}$

S: start symbol

a: a terminal symbol

A: a non-terminal symbol

α, β : a string composed of terminals and non-terminals (typically, α is the RHS of a production)

\Rightarrow : derived in 1 step

\Rightarrow^* : derived in 0 or more steps

\Rightarrow^+ : derived in 1 or more steps

Computing first sets

- Terminal: $\text{First}(a) = \{a\}$
- Non-terminal: $\text{First}(A)$
 - Look at all productions for A
 $A \rightarrow X_1 X_2 \dots X_k$
 - $\text{First}(A) \supseteq (\text{First}(X_1) - \lambda)$
 - If $\lambda \in \text{First}(X_1)$, $\text{First}(A) \supseteq (\text{First}(X_2) - \lambda)$
 - If λ is in $\text{First}(X_i)$ for all i , then $\lambda \in \text{First}(A)$
- Computing $\text{First}(\alpha)$: similar procedure to computing $\text{First}(A)$

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$

$B \rightarrow \lambda$

• A sentence in the grammar:

$x a c c \$$

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$

$B \rightarrow \lambda$

- A sentence in the grammar:

$x a c c \$$

special "end of input" symbol

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$ • A sentence in the grammar:

$B \rightarrow \lambda$ $x a c c \$$

Current derivation: S

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$

$B \rightarrow \lambda$

• A sentence in the grammar:

$x a c c \$$

Current derivation: $A B c \$$

Predict rule

A simple example

$S \rightarrow A B c \$$

Choose based on
first set of rules

$A \rightarrow x a A$
 $A \rightarrow y a A$
 $A \rightarrow c$

$B \rightarrow b$

• A sentence in the grammar:

$B \rightarrow \lambda$

$x a c c \$$

Current derivation: $x a A B c \$$

Predict rule *based on next token*

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$ • A sentence in the grammar:

$B \rightarrow \lambda$ $x a c c \$$

Current derivation: $x a A B c \$$

Match token

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

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Match token

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$A \rightarrow x a A$
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Predict rule *based on next token*

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$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$ • A sentence in the grammar:

$B \rightarrow \lambda$ $x a c c \$$

Current derivation: $x a c B c \$$

Match token

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

Choose based on
follow set

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$

$B \rightarrow \lambda$

• A sentence in the grammar:

$x a c c \$$

Current derivation: $x a c \lambda c \$$

Predict rule *based on next token*

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$ • A sentence in the grammar:

$B \rightarrow \lambda$ $x a c c \$$

Current derivation: $x a c c \$$

Match token

A simple example

$S \rightarrow A B c \$$

$A \rightarrow x a A$

$A \rightarrow y a A$

$A \rightarrow c$

$B \rightarrow b$ • A sentence in the grammar:

$B \rightarrow \lambda$ $x a c c \$$

Current derivation: $x a c c \$$

Match token

Top-down Parsing

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- 2) $S \rightarrow (S + F)$
- 3) $F \rightarrow a$

string: (a+a)

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Towards parser generators

- Key problem: as we read the source program, we need to decide what productions to use
- Step 1: find the tokens that can tell which production P (of the form $A \rightarrow X_1 X_2 \dots X_m$) applies

$\text{Predict}(P) =$

$$\begin{cases} \text{First}(X_1 \dots X_m) & \text{if } \lambda \notin \text{First}(X_1 \dots X_m) \\ (\text{First}(X_1 \dots X_m) - \lambda) \cup \text{Follow}(A) & \text{otherwise} \end{cases}$$

- If next token is in $\text{Predict}(P)$, then we should choose this production