CS406: Compilers Spring 2021

Week 12: Control Flow Graphs, Data Flow Analysis

Basic Blocks and Flow Graphs

- Basic Block
	- Maximal sequence of consecutive instructions with the following properties:
		- The first instruction of the basic block is the *only entry point*
		- The last instruction of the basic block is either the halt instruction or the *only exit point*
- Flow Graph
	- Nodes are the basic blocks
	- Directed edge indicates which block follows which block

Basic Blocks and Flow Graphs - Example

A data flow graph

Flow Graphs

- Capture how control transfers between basic blocks due to:
	- Conditional constructs
	- Loops
- Are necessary when we want optimize considering larger parts of the program
	- Multiple procedures
	- Whole program

Flow Graphs - Representation

- We need to label and track statements that are jump targets
	- **Explicit targets** targets mentioned in jump statement
	- **Implicit targets** targets that follow conditional jump statement
		- Statement that is executed if the branch is not taken
- Implementation
	- Linked lists for BBs
	- Graph data structures for flow graphs

$$
A = 4
$$

\nt1 = A * B
\nrepeat {
\nt2 = t1/C
\nif (t2 \geq W) {
\nM = t1 * k
\nt3 = M + I
\n}
\nH = I
\nM = t3 - H
\n3 until (T3 \geq 0)

CFG for running example

Constructing a CFG

- To construct a CFG where each node is a basic block
	- Identify *leaders*: first statement of a basic block
	- In program order, construct a block by appending subsequent statements up to, but not including, the next leader
- Identifying leaders
	- First statement in the program
	- Explicit target of any conditional or unconditional branch
	- Implicit target of any branch

Partitioning algorithm

- Input: set of statements, $stat(i)$ = ith statement in input
- Output: set of leaders, set of basic blocks where $block(x)$ is the set of statements in the block with leader x
- Algorithm

```
leads = \{1\} //Leaders always includes first statement
for i = 1 to |n| //|n| = number of statements
   if stat(i) is a branch, then
      leaders = leaders \cup all potential targets
end for
worklist = leaders
while worklist not empty do
   x = remove earliest statement in worklist
   block(x) = \{x\}for (i = x + 1; i \leq |n| and i \notin leaders; (i++)block(x) = block(x) \cup \{i\}end for
end while
```
Leaders = Basic blocks =

Leaders = ${1}$
Basic blocks =

Leaders = ${1}$
Basic blocks =

$$
A = 4
$$
\n
$$
\begin{array}{rcl}\n1 & A & = & 4 \\
2 & t1 & = & A * & B \\
\hline\n3 & L1: & t2 & = & t1 / C \\
4 & if & t2 & < W \text{ goto } L2 \\
5 & M & = & t1 * & k \\
6 & t3 & = & M + I \\
7 & L2: & H = I \\
8 & M & = & t3 - H \\
9 & if & t3 & \geq 0 \text{ goto } L3 \\
10 & \text{goto } L1\n\end{array}
$$
\n
$$
11 \quad L3: \text{ halt}
$$

Leaders = ${1, 3}$
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ goto L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ goto L3
\n10 g oto L1
\n11 $L3$: halt

Leaders = ${1, 3}$
Basic blocks =

Leaders = ${1, 3, 5}$
Basic blocks =

$$
A = 4
$$
\n
$$
2 \quad t1 = A * B
$$
\n
$$
3 \quad L1: \quad t2 = t1 / C
$$
\n
$$
4 \quad \text{if } t2 < W \text{ go to } L2
$$
\n
$$
5 \quad M = t1 * k
$$
\n
$$
6 \quad t3 = M + I
$$
\n
$$
7 \quad L2: \quad H = I
$$
\n
$$
8 \quad M = t3 - H
$$
\n
$$
9 \quad \text{if } t3 \ge 0 \text{ go to } L3
$$
\n
$$
10 \quad \text{go to } L1
$$
\n
$$
11 \quad L3: \text{ halt}
$$

Leaders = ${1, 3, 5}$ Basic blocks $=$

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 L1: $t2 = t1 / C$
\n4 if $t2 < W$ goto L2
\n5 M = t1 * k
\n6 t3 = M + I
\n7 L2: H = I
\n8 M = t3 - H
\n9 if $t3 \ge 0$ goto L3
\n10 goto L1
\n11 L3: halt

Leaders = ${1, 3, 5, 7}$ Basic blocks =

Leaders = ${1, 3, 5, 7}$ Basic blocks =

Leaders = ${1, 3, 5, 7}$ Basic blocks =

Leaders = ${1, 3, 5, 7, 10}$ Basic blocks =

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Basic blocks =

$$
A = 4
$$
\n
$$
B = 4
$$
\n
$$
C = 1
$$
\n
$$
C =
$$

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block (1) = ?
Basic blocks =

Leaders = $\{1,3,5,7,10,11\}$ Block(1) = ?
Basic blocks =

24 Start from statement 2 and add till either the end or a leader is reached

Leaders = $\{1,3,5,7,10,11\}$ Block(1) = $\{1,2\}$
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ go to L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ go to L3
\n10 g oto L1
\n11 $L3$: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(3) = ?
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ goto L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ goto L3
\n10 $g \text{oto } L1$
\n11 $L3$: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(3) = $\{3,4\}$
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ go to L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ go to L3
\n10 g oto L1
\n11 $L3$: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(5) = ?
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ goto L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ goto L3
\n10 $g \text{oto } L1$
\n11 $L3$: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(5) = $\{5,6\}$
Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 $L1$: $t2 = t1 / C$
\n4 $i f t2 < W$ go to L2
\n5 $M = t1 * k$
\n6 $t3 = M + I$
\n7 $L2$: $H = I$
\n8 $M = t3 - H$
\n9 $i f t3 \ge 0$ go to L3
\n10 $g \text{oto } L1$
\n11 $L3$: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(7) = ? Basic blocks =

1
$$
A = 4
$$

\n2 $t1 = A * B$
\n3 L1: $t2 = t1 / C$
\n4 if $t2 < W$ go to L2
\n5 M = t1 * k
\n6 t3 = M + I
\n7 L2: H = I
\n8 M = t3 - H
\n9 if $t3 \ge 0$ go to L3
\n10 go to L1
\n11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(7) = $\{7,8,9\}$
Basic blocks =

Leaders = $\{1,3,5,7,10,11\}$ Block(10) = ?
Basic blocks =

Leaders = $\{1,3,5,7,10,11\}$ Block(10) = $\{10\}$
Basic blocks =

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(11) = $\{11\}$
Basic blocks =

1	$A = 4$
2	$t1 = A * B$
3	$L1$: $t2 = t1 / C$
4	$i f t2 < W goto L2$
5	$M = t1 * k$
6	$t3 = M + I$
7	$L2$: $H = I$
8	$M = t3 - H$
9	$i f t3 \ge 0 goto L3$
10	$goto L1$
11	$L3$: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Basic blocks = {{1, 2}, {3, 4}, {5, 6}, {7, 8, 9}, {10}, {11} }

Putting edges in CFG

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks
- Output: The CFG

for $i = 1$ to $|block|$ {{1,2},{3,4},{5,6},{7,8,9},{10},{11}} $x =$ last statement of block(i) **if** stat(x) is a branch, **then for** each explicit target y of stat(x) create edge from block *i* to block y end for **if** stat(x) is not unconditional **then** create edge from block *i* to block *i*+1 end for
- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B₂
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B₂
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

- There is a directed edge from B_1 to B_2 if
	- There is a branch from the last statement of B_1 to the first statement (leader) of B_2
	- B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: block, a sequence of basic blocks

Result

Discussion

- \bullet Some times we will also consider the statement-level CFG, where each node is a statement rather than a basic block
	- Either kind of graph is referred to as a CFG
- In statement-level CFG, we often use a node to explicitly represent merging of control
	- Control merges when two different CFG nodes point to the same node
- Note: if input language is structured, front-end can generate basic block directly
	- "GOTO considered harmful"

Statement level CFG

Control Flow Graphs - Use

- Why do we need CFGs? Global Optimization
	- Optimizing compilers do global optimization (i.e. optimize beyond basic blocks)
		- Differentiating aspect of normal and optimizing compilers
	- E.g. loops are the most frequent targets of global optimization (because they are often the "hot-spots" during program execution)

how do we identify loops in CFGs?

- Loops **how do we identify loops in CFGs?** For a set of nodes, L, that belong to loop:
	- 1) There is a *loop entry node* such that any path from the *graph entry node* to any node in L goes through the *loop entry node.* i.e. no node in L has a predecessor that is outside L.
	- *2) Every node in L* has a non-empty path, completely within L, to the entry of L.

Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?

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Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?

- 1) Is $L = {B2, B4, B5}$ a loop?. No. Consider:
	- There is a *loop entry node* such that any path from the *graph entry node* to any node in L goes through the *loop entry node.* i.e. no node in L has a predecessor that is outside L.

- 1) Is $L = {B2, B4, B5}$ a loop?. No. Consider:
	- *Every node in L* has a non-empty path, completely within L, to the entry of L.

1) Is L={B2, B3, B4, B5} a loop?.

Optimize Loops

• Example - Code Motion Should be careful while doing optimization of loops

```
while J > I loop
  A(j) := 10/I;j := j + 2;end loop;
```
Optimize Loops – Code Motion

• Should be careful while doing optimization of loops

> **while** J > I **loop** $A(j) := 10/I;$ $j := j + 2;$ **end loop;**

• Optimization: can move 10/I out of loop.

Optimize Loops – Code Motion

• Should be careful while doing optimization of loops

> **while** J > I **loop** $A(j) := 10/I;$ $j := j + 2;$ **end loop;**

- Optimization: can move 10/I out of loop
- What if $I = 0$?

Optimize Loops – Code Motion

• Should be careful while doing optimization of loops

> **while** J > I **loop** $A(j) := 10/I;$ $j := j + 2;$ **end loop;**

- Optimization: can move 10/I out of loop
- What if $I = 0$?
- What if I != 0 but loop executes zero times?

Optimization Criteria - Safety and Profitability

- Safety is the code produced after optimization producing same result?
- Profitability is the code produced after optimization running faster or uses less memory or triggers lesser number of page faults etc.

$$
\begin{array}{rcl}\n\text{while } J > I \text{ loop} \\
\text{A(j)} &:= 10/I; \\
\text{j} &:= j + 2; \\
\text{end loop;} \n\end{array}
$$

- E.g. moving I out of the loop introduces exception (when I=0)
- E.g. if the loop is executed zero times, moving I out is not profitable

- How do we identify expressions that can be moved out of the loop?
	- LoopDef = $\{\}$ set of variables defined i.e. whose values are overwritten) in the loop body
	- LoopUse = $\{ \}$ 'relevant' variables used in computing an expression

Mark_Invariants(Loop L) {

}

- 1. Compute LoopDef for L
- 2. Mark as invariant all expressions, whose relevant variables don't belong to LoopDef

• Example

LoopDef{}

for I = 1 **to** 100 **for** J = 1 **to** 100 **for** K = 1 **to** $100 A[I][J][K] = (I * J) * K$ $\rightarrow \{A, K\}$ $\rightarrow \{A, J, K\}$ {A, J, K}

• Example

Invariant Expressions

for I = 1 **to** 100 **for** J = 1 **to** 100 for K = 1 to 100 \longrightarrow { $I*J$, $A[I][J][K] = (I * J) * K$ $Addr(A[i][j])$

For an array access, $A[m] \Rightarrow Addr(A) + m$ For 3D array above*, $Addr(A[I][J][K]) =$ **Addr(A)+(I*10000)-10000+(J*100)-100+K-1**

*Assuming row-major ordering of storage

• Example **for** I = 1 **to** 100 **for** J = 1 **to** 100 **for** K = 1 **to** 100 $A[I][J][K] = (I * J) * K$ Invariant Expressions { Addr(A[i]) }

For an array access, $A[m] \Rightarrow Addr(A) + m$ For 3D array above*, $Addr(A[\Pi][J][K]) =$ **Addr(A)+(I*10000)-10000+(J*100)-100+K-1**

*Assuming row-major ordering of storage

• Move the invariant expressions identified

Factor_Invariants(Loop L) { Mark Invariants(L); **foreach** expression E marked an invariant:

1. Create a temporary T

}

- 2. Replace each occurrence of E in L with T
- 3. Insert T:=E in L's header code immediately **after** the first looptermination test (i.e. after "j<!op> OUT" in slide 39, week9.pdf) // If loop is known to execute at least once,

insert T:=E **before** LOOP:

• Example

for I = 1 **to** 100 **for** J = 1 **to** 100 **for** K = 1 **to** 100 $A[I][J][K] = (I * J) * K$ **for** I=1 **to** 100 temp3=Addr(A[i]) **for** J=1 **to** 100 temp1=Addr(temp3(J)) temp2=I*J **for** K=1 **to** 100 $temp1[K]=temp2*K$

• Expressions cannot always be moved out!

Case I: We can move $t = a$ op b if the statement dominates all loop exits where t is live

A node a dominates node b if all paths to b must go through a

$$
for (...) {\nif(*)\na = 100\n}\nC=a
$$

Cannot move a=100 because it does not dominate c=a i.e. there is one path (when if condition is false) $c=a$ can be reached without going $a=100$

• Expressions cannot always be moved out!

Case II: We can move $t = a$ op b if there is only definition of t in the loop

$$
for (...) {\nif(*)\na = 100\nelse\na = 200\n}
$$

Multiple definition of a

• Expressions cannot always be moved out!

Case III: We can move t = a op b if t is not defined before the loop, where the definition reaches t's use after the loop

a=5 **for** (...) { a = 4+b } c=a

Definition of a in $a=5$ reaches $c=a$, which is defined after the loop

Optimize Loops –Strength Reduction

- Like strength reduction in peephole optimization
	- E.g. replace $a*2$ with $a<<1$
- Applies to uses of induction variable in loops
	- Basic induction variable (I) only definition within the loop is of the form $I = I \pm S$, (S is loop invariant)

I *usually determines number of iterations*

- Mutual induction variable (J) defined within the loop, its value is linear function of other induction variable, I, such that
	- $J = I * C \pm D$ (C, D are loop invariants)

Optimize Loops –Strength Reduction

strength_reduce(Loop L) { Mark Invariants(L); **foreach** expression E of the form I*C+D where I is L's loop index and C and D are loop invariants 1. Create a temporary T 2. Replace each occurrence of E in L with T

- 3. Insert $T := I_0^*C + D$, where I_0 is the initial value of the induction variable, immediately before L
- 4. Insert $T: = T + S * C$, where S is the step size, at the end of L's body
- }

Optimize Loops –Strength Reduction

- Suppose induction variable I takes on values I_{o} , $I_0 + S$, $I_0 + 2S$, $I_0 + 3S$... in iterations 1, 2, 3, 4, and so on…
- Then, in consecutive iterations, Expression I*C+D takes on values

$$
I_0 * C + D
$$

($I_0 + S$) * $C + D$ = $I_0 * C + S * C + D$
($I_0 + 2S$) * $C + D$ = $I_0 * C + 2S * C + D$

- The expression changes by a constant S*C
- Therefore, we have replaced a $*$ and + with a +

Optimize Loops – Strength Reduction

• Example (Applying to innermost loop)

71 **for** I = 1 **to** 100 **for** J = 1 **to** 100 **for** K = 1 **to** 100 $A[I][J][K] = (I * J) * K$ **for** I=1 **to** 100 temp3=Addr(A[i]) **for** J=1 **to** 100 temp1=Addr(temp3(J)) temp2=I*J **for** K=1 **to** 100 $temp1[K]=temp2*K$. . . temp2=I*J temp4=temp2 **for** K=1 **to** 100 $temp1[K] = temp4$ temp4=temp4+temp2 $//S=1$ //C=temp2

Optimize Loops – Strength Reduction

• Exercise (Apply to intermediate loop)

Optimize Loops – Strength Reduction

• Exercise (Apply to intermediate loop)

```
...
. . .
temp5=I
for J=1 to 100
     temp1=Addr(temp3(J))
     temp2=temp5
     temp4=temp2
     for K=1 to 100
        temp1[K]=temp4temp4=temp4+temp2
     temp5=temp5+I
                                      ...
```
Optimize Loops – Strength Reduction

• Further strength reduction possible?

```
for I=1 to 100
  temp3=Addr(A[i])
  temp5=I
  for J=1 to 100
     temp1=Addr(temp3(J))
     temp2=temp5
     temp4=temp2
     for K=1 to 100
        temp1[K]=temp4temp4=temp4+temp2
     temp5=temp5+I
```
Optimize Loops – Loop Unrolling

- Modifying induction variable in each iteration can be expensive
- Can instead unroll loops and perform multiple iterations for each increment of the induction variable
- What are the advantages and disadvantages?

for (i = 0; i < N; i++) $A[i] = \ldots$ Unroll by factor of 4 for $(i = 0; i < N; i += 4)$ $A[i] = ...$ $A[i+1] = \ldots$ $A[i+2] = ...$ $A[i+3] = ...$

Optimize Loops - Summary

- Low level optimization
	- Moving code around in a single loop
	- Examples: loop invariant code motion, strength reduction, loop unrolling
- High level optimization
	- Restructuring loops, often affects multiple loops
	- Examples: loop fusion, loop interchange, loop tiling

Useful optimizations

- Common subexpression elimination (global)
	- Need to know which expressions are available at a point
- Dead code elimination
	- Need to know if the effects of a piece of code are never needed, or if code cannot be reached
- Constant folding
	- Need to know if variable has a constant value
- So how do we get this information?

Dataflow analysis

- Framework for doing compiler analyses to drive optimization
- Works across basic blocks
- **Examples** \bullet
	- Constant propagation: determine which variables are constant
	- Liveness analysis: determine which variables are live
	- Available expressions: determine which expressions are have valid computed values
	- Reaching definitions: determine which definitions could "reach" a use

Liveness – Recap..

X is live at 1 ..used in future

$$
N: Y = X + 5
$$

X used here

……

- A variable X is live at statement S if:
	- There is a statement S' that uses X
	- There is a path from S to S'
	- There are no intervening definitions of X

Liveness – Recap..

- 1: X = 10 X is **dead** at 1 $2: X = Y + 2$ $…_•$ $N: Y = X + 5$
- A variable X is dead at statement S if it is not live at S
	- What about \ldots ; $X = X + 1$?

• Define a set LiveIn(b), where b is a basic block, as: the set of all variables live at the entrance of a basic block

• Define a set Def(b), where b is a basic block, as: the set of all variables that are defined within block b

• Define a set LiveOut(b), where b is a basic block, as: the set of all variables live at the exit of a basic block

• If $S(b)$ is the set of all successors of b, then

LiveOut(b) = $U_i \in S(b)$ LiveIn(i)

• Define a set LiveUse(b), where b is a basic block, as: the set of all variables that are used within block b. LiveIn(b) \supseteq LiveUse(b)

Liveness in a CFG - Observation

•If a node neither uses nor defines X, the liveness property remains the same before and after executing the node

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

LiveIn(b)⊇ LiveOut(b) – Def(b)

•Under what scenarios can a variable be live at the entrance of a basic block?

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

LiveIn(b)⊇ LiveOut(b) – Def(b)

•Under what scenarios can a variable be live at the entrance of a basic block?

•Either the variable is used in the basic block

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

LiveIn(b)⊇ LiveOut(b) – Def(b)

•Under what scenarios can a variable be live at the entrance of a basic block?

•Either the variable is used in the basic block •OR the variable is live at exit and not defined within the block

•Under what scenarios can a variable be live at the entrance of a basic block?

•Either the variable is used in the basic block •OR the variable is live at exit and not defined within the block

 $LiveIn(b) = LiveUse(b) \cup (LiveOut(b) Def(b)$)

• Draw CFG for the code:

 $A: = 1$ **if** A=B **then** B:=1 **else** $C: = 1$ **endif** $D:=A+B$

• start from use of a variable to its definition. Is this analysis going backward or forward w.r.t. control flow?

• start from use of a variable to its definition. *Backward-flow problem*

• Start from use of a variable to its definition. •Compute:

 $LiveIn(b) = LiveUse(b) \cup (LiveOut(b) - Def(b))$

• Start from use of a variable to its definition. •Compute:

 $LiveIn(b) = LiveUse(b) \cup (LiveOut(b) - Def(b))$

• Assume that the CFG below represents *your entire program* •What can you infer from the table?

• Assume that the CFG below represents *your entire program* •Variable B is live in b1, the entry basic block of CFG. This implies that B is used before it is defined. An error!

