CS323: Compilers Spring 2023

Week 11: Instruction Scheduling (contd..), Control Flow Graphs

Acknowledgements: Milind Kulkarni

List scheduling - Example



List scheduling

LD A, R I
 LD B, R2
 R3 = RI + R2
 LD C, R4
 R5 = R4 * R2
 R6 = R3 + R5
 ST R6, D

Cycle	ALU0	ALUI	LD/ST
0			I
			I
2			2
3			2
4	3		4
5			4
6	5		
7			
8	6		
9			7
10			

Height-based scheduling

- Important to prioritize instructions
 - Instructions that have a lot of downstream instructions dependent on them should be scheduled earlier
- Instruction scheduling NP-hard in general, but heightbased scheduling is effective
- Instruction height = latency from instruction to farthest-away leaf
 - Leaf node height = instruction latency
 - Interior node height = max(heights of children + instruction latency)
- Schedule instructions with highest height first



Height-based list scheduling

LD A, RI
 LD B, R2
 R3 = RI + R2
 LD C, R4
 R5 = R4 * R2
 R6 = R3 + R5
 ST R6, D

Cycle	ALU0	ALUI	LD/ST
0			2
I			2
2			4
3			4
4	5		I
5			I
6	3		
7	6		
8	7		
9			
10			

Instruction Scheduling - Exercise

•2 ALUs (fully pipelined) and one LD/ST unit (not pipelined) are available.
•Either of the ALUs can execute ADD (1 cycle). Only one of the ALUs can execute MUL (2 cycles).

•LDs take up an ALU for 1 cycle and LD/ST unit for two cycles.

•STs take up an ALU for 1 cycle and LD/ST unit for one cycle.

i) Draw reservation tables, *ii*)DAG for the code shown *iii*) schedule using height based list scheduling.

Ε

1:	LD	Α	R1			11:	ST	R10	
2:	LD	В	R2			12:	ST	R7	ł
3:	LD	С	R3						
4:	LD	D	R4						
5:	R5	=	R1	+	R2				
6:	R6	=	R5	*	R3				
7:	R7	=	R1	+	R6				
8:	R8	=	R6	+	R5				
9:	R9	=	R4	+	R7				
10	• R1	10	= F	29	+ R8				

Basic Blocks and Flow Graphs

- Basic Block
 - Maximal sequence of consecutive instructions with the following properties:
 - The first instruction of the basic block is the *only entry point*
 - The last instruction of the basic block is either the halt instruction or the *only exit point*
- Flow Graph
 - Nodes are the basic blocks
 - Directed edge indicates which block follows which block

Basic Blocks and Flow Graphs - Example



A data flow graph

Flow Graphs

- Capture how control transfers between basic blocks due to:
 - Conditional constructs
 - Loops
- Are necessary when we want optimize considering larger parts of the program
 - Multiple procedures
 - Whole program

Flow Graphs - Representation

- We need to label and track statements that are jump targets
 - Explicit targets targets mentioned in jump statement
 - Implicit targets targets that follow conditional jump statement
 - Statement that is executed if the branch is not taken
- Implementation
 - Linked lists for Basic Blocks
 - Graph data structures for flow graphs

A = 4
t1 = A * B
repeat {
t2 = t1/C
if (t2
$$\ge$$
 W) {
M = t1 * k
t3 = M + I
}
H = I
M = t3 - H
} until (T3 \ge 0)

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

CFG for running example



Constructing a CFG

- To construct a CFG where each node is a basic block
 - Identify *leaders*: first statement of a basic block
 - In program order, construct a block by appending subsequent statements up to, but not including, the next leader
- Identifying leaders
 - First statement in the program
 - Explicit target of any conditional or unconditional branch
 - Implicit target of any branch

Partitioning algorithm

- Input: set of statements, stat(i) = ith statement in input
- Output: set of leaders, set of basic blocks where block(x) is the set of statements in the block with leader x
- Algorithm

```
leaders = {1} //Leaders always includes first statement
for i = 1 to |n| //|n| = number of statements
if stat(i) is a branch, then
leaders = leaders ∪ all potential targets
end for
worklist = leaders
while worklist not empty do
x = remove earliest statement in worklist
block(x) = {x}
for (i = x + 1; i ≤ |n| and i ∉ leaders; i++)
block(x) = block(x) ∪ {i}
end for
end while
```



1		A = 4
2		t1 = A * B
3	L1:	t2 = t1 / C
4		if t2 < W goto L2
5		M = t1 * k
6		t3 = M + I
7	L2:	H = I
8		M = t3 - H
9		if t3 ≥ 0 goto L3
10		goto L1
11	L3:	halt

Leaders = {1} Basic blocks =

Leaders = {1} Basic blocks =

Leaders = $\{1,3\}$ Basic blocks =

Leaders = $\{1,3\}$ Basic blocks =

Leaders = $\{1,3,5\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto L1$
11 L3: halt

Leaders = $\{1,3,5,7\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10\}$ Basic blocks =



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1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(1) = ? Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = {1,3,5,7,10,11} Basic blocks =

Block(1) = ? Start from statement 2 and add till either the end or a leader is reached ³⁰

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1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(1) = $\{1, 2\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(3) = ? Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(3) = $\{3, 4\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(5) = ? Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(5) = $\{5,6\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(7) = ? Basic blocks =
1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(7) = $\{7,8,9\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(10) = ? Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto \ L1$
11 L3: halt

Leaders = $\{1,3,5,7,10,11\}$ Block(10) = $\{10\}$ Basic blocks =

1
$$A = 4$$

2 $t1 = A * B$
3 L1: $t2 = t1 / C$
4 $if t2 < W \text{ goto } L2$
5 $M = t1 * k$
6 $t3 = M + I$
7 L2: $H = I$
8 $M = t3 - H$
9 $if t3 \ge 0 \text{ goto } L3$
10 $goto L1$
11 L3: halt

Leaders = $\{1, 3, 5, 7, 10, 11\}$ Block(11) = $\{11\}$ Basic blocks =

Leaders = {1, 3, 5, 7, 10, 11} Basic blocks = { {1, 2}, {3, 4}, {5, 6}, {7, 8, 9}, {10}, {11} }

- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B₂ immediately follows B₁ in program order and B₁ does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

for i = I to |block| {{1,2},{3,4},{5,6},{7,8,9},{10},{11}}
x = last statement of block(i)
if stat(x) is a branch, then
for each explicit target y of stat(x)
 create edge from block i to block y
end for
if stat(x) is not unconditional then
create edge from block i to block i+1
end for

- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B₂ immediately follows B₁ in program order and B₁ does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B₂ immediately follows B₁ in program order and B₁ does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B_1 to B_2 if
 - There is a branch from the last statement of B_1 to the first statement (leader) of B₂
 - B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B₂ immediately follows B₁ in program order and B₁ does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B2 immediately follows B1 in program order and B1 does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B_1 to B_2 if
 - There is a branch from the last statement of B_1 to the first statement (leader) of B₂
 - B_2 immediately follows B_1 in program order and B_1 does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



- There is a directed edge from B1 to B2 if
 - There is a branch from the last statement of B₁ to the first statement (leader) of B₂
 - B₂ immediately follows B₁ in program order and B₁ does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks



Result



Discussion

- Some times we will also consider the *statement-level* CFG, where each node is a statement rather than a basic block
 - Either kind of graph is referred to as a CFG
- In statement-level CFG, we often use a node to explicitly represent *merging* of control
 - Control merges when two different CFG nodes point to the same node
- Note: if input language is structured, front-end can generate basic block directly
 - "GOTO considered harmful"

Statement level CFG



Control Flow Graphs - Use

- Why do we need CFGs? Global Optimization
 - Optimizing compilers do global optimization (i.e. optimize beyond basic blocks)
 - Differentiating aspect of normal and optimizing compilers
 - E.g. loops are the most frequent targets of global optimization (because they are often the "hot-spots" during program execution)

how do we identify loops in CFGs?

- Loops how do we identify loops in CFGs? For a set of nodes, L, that belong to loop:
 - 1) There is a *loop entry node* with the property that no other node in L has a predecessor outside L. That is, every path from entry of the entire flow graph (*graph entry node*) to any node in L goes through the loop entry node.
 - 2) Every node in L has a non-empty path, completely within L, to the entry of L.



Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?



Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?

1) Is L={B2, B4, B5} a loop?. No. Consider:

1) There is a *loop entry node* with the property that no other node in L has a predecessor outside L. That is, every path from entry of the entire flow graph (*graph entry node*) to any node in L goes through the loop entry node.



- 1) Is L={B2, B4, B5} a loop?. No. Consider:
 - *Every node in L* has a non-empty path, completely within L, to the entry of L.



1) Is L={B2, B3, B4, B5} a loop?.



Optimizing Loops

Optimize Loops

Example - Code Motion
 Should be careful while doing optimization of loops

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

while J > I loop
 A(j) := 10/I;
 j := j + 2;
end loop;

• Optimization: can move 10/I out of loop.

Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

while J > I loop
 A(j) := 10/I;
 j := j + 2;
end loop;

- Optimization: can move 10/I out of loop
- What if I = 0?

Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

while J > I loop
 A(j) := 10/I;
 j := j + 2;
end loop;

- Optimization: can move 10/I out of loop
- What if I = 0?
- What if I != 0 but loop executes zero times?

Optimization Criteria - Safety and Profitability

- Safety is the code produced after optimization producing same result?
- Profitability is the code produced after optimization running faster or uses less memory or triggers lesser number of page faults etc.

- E.g. moving I out of the loop introduces exception (when I=0)
- E.g. if the loop is executed zero times, moving A(j) := 10/I out is not profitable

Optimize Loops – Code Generation

• The outline of code generation for 'for' loops looked like this:

```
for (<init_stmt>; <bool_expr>; <incr_stmt>)
                                             for (i=0; i<=255;i++) {
  <stmt_list>
                                                  <stmt list>
end
                                              }
                                                             Naïve code generation
                                              code for i=0;
                                              code for i<=255
                                     LOOP:
               <init_stmt>
                                              jump0 OUT
             LOOP:
                                              code for <stmt list>
               <bool_expr>
               j<!op> OUT
                                     INCR:
                                              code for i++
               <stmt_list>
                                              jump LOOP
             INCR:
                                     OUT:
               <incr_stmt>
               jmp LOOP
                                      Question: why naïve is not good?
             OUT:
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                                                                           66
```

Optimize Loops – Code Generation

 What happens when ub is set to the maximum possible integer representable by the type of i?

```
for (i=0; i<=255;i++) {
          <stmt list>
      }
                                                   code for i=0;
                    Better code:
                                                   compute 1b, ub
        code for i=0;
                                                   code for lb<=ub</pre>
        code for 1b=0, ub=255
                                                   jump0 OUT
        code for lb<=ub</pre>
                                                   assign index=1b
        jump0 OUT
                                                   assign limit=ub
LOOP: code for <stmt_list>
                                           LOOP:
                                                   code for <stmt list>
        code for i=ub
                                                   code for index=limit
                                generalizing:
        jump1 OUT
                                                   jump1 OUT
INCR:
        code for i++
                                           INCR:
                                                   code for increment index
        jump LOOP
                                                   jump LOOP
OUT:
                                          OUT:
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                                                                       67
```

- How do we identify expressions that can be moved out of the loop?
 - LoopDef = {} set of variables <u>defined</u> (i.e. whose values are overwritten) in the loop body
 - LoopUse = { } 'relevant' variables <u>used in</u> computing an expression

Mark_Invariants(Loop L) {

- 1. Compute LoopDef for L
- 2. Mark as invariant all expressions, whose relevant variables don't belong to LoopDef

• Example

LoopDef{}

for I = 1 to 100 \longrightarrow {A, J, K, I} for J = 1 to 100 \longrightarrow {A, J, K} for K = 1 to 100 \longrightarrow {A, K} A[I][J][K] = (I*J)*K

• Example

LoopUse{}

for I = 1 to 100 \longrightarrow {} for J = 1 to 100 \longrightarrow {I} for K = 1 to 100 \longrightarrow {I,J} A[I][J][K] = (I*J)*K

• Example

Invariant Expressions

for I = 1 to 100
 for J = 1 to 100
 for K = 1 to 100 → { I*J,
 A[I][J][K] = (I*J)*K Addr(A[i][j])}

For an array access, A[m] => Addr(A) + m

For 3D array above*, Addr(A[I][J][K]) =
 Addr(A)+(I*10000)-1000+(J*100)-100+K-1

 Example
 Invariant Expressions
 for I = 1 to 100 for J = 1 to 100 for K = 1 to 100 A[I][J][K] = (I*J)*K

For an array access, A[m] => Addr(A) + m
For 3D array above*, Addr(A[I][J][K]) =
 Addr(A)+(I*10000)-10000+(J*100)-100+K-1
• Move the invariant expressions identified

Factor_Invariants(Loop L) { Mark_Invariants(L); foreach expression E marked an invariant: 1. Create a temporary T 2. Replace each occurrence of E in L with T 3. Insert T:=E in L's header code //If loop is known to execute at least once, insert T:=E before LOOP:

• Example

//Invariant Expressions

• Example

• Example

• Expressions cannot always be moved out!

Case I: We can move t = a op b if the statement <u>dominates</u> all loop exits where t is live

A node bb1 dominates node bb2 if all paths to bb2 must go through bb1

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Cannot move a=100 because it does not dominate c=a i.e. there is one path (when if condition is false) c=a can be executed /'reached' without going to a=100

Expressions cannot always be moved out!

Case II: We can move t = a op b if there is only one definition of t in the loop

Multiple definition of a

Expressions cannot always be moved out!
 Case III: We can move t = a op b if t is not defined before the loop, where the definition reaches t's use

after the loop

Definition of a in a=5 reaches c=a, which is defined after the loop

- Like strength reduction in peephole optimization
 - E.g. replace a*2 with a<<1
- Applies to uses of induction variable in loops
 - Basic induction variable (I) only definition within the loop is of the form I = I ± S, (S is loop invariant)

I usually determines number of iterations

- Mutual induction variable (J) defined within the loop, its value is linear function of other induction variable, I, such that
 - J = I * C ± D (C, D are loop invariants)

strength_reduce(Loop L) { Mark_Invariants(L); foreach expression E of the form I*C+D where I is L's loop index and C and D are loop invariants 1. Create a temporary T 2. Replace each occurrence of E in L with T

- 3. Insert $T:=I_o*C+D$, where I_o is the initial value of the induction variable, immediately before L
- 4. Insert T:=T+S*C, where S is the step size, at the end of
 L's body
- }

- Suppose induction variable I takes on values I_o, I_o+S, I_o+2S, I_o+3S... in iterations 1, 2, 3, 4, and so on...
- Then, in consecutive iterations, Expression I*C+D takes on values

$$I_{o}^{*}C+D$$

($I_{o}^{+}S$)*C+D = $I_{o}^{*}C+S^{*}C+D$
($I_{o}^{+}2S$)*C+D = $I_{o}^{*}C+2S^{*}C+D$

- The expression changes by a constant S*C
- Therefore, we have replaced a * and + with a +

• Example (Applying to innermost loop)

for I = 1 to 100 for I=1 to 100 for J = 1 to 100 temp3=Addr(A[i]) for K = 1 to 100 for J=1 to 100 A[I][J][K] = (I*J)*Ktemp1=Addr(temp3(J)) temp2=I*J for K=1 to 100 temp1[K]=temp2*K temp2=I*J temp4=temp2 for K=1 to 100 //S=1 temp1[K]=temp4 //C=temp2 temp4=temp4+temp2 CS406. IIT Dharwad 83

• Exercise (Apply to intermediate loop)



• Exercise (Apply to intermediate loop)

```
. . .
temp5=I
for J=1 to 100
      temp1=Addr(temp3(J))
      temp2=temp5
      temp4=temp2
      for K=1 to 100
         temp1[K]=temp4
         temp4=temp4+temp2
      temp5=temp5+I
   CS406, IIT Dharwad
```

• Further strength reduction possible?

```
for I=1 to 100
  temp3=Addr(A[i])
  temp5=I
  for J=1 to 100
     temp1=Addr(temp3(J))
     temp2=temp5
     temp4=temp2
     for K=1 to 100
        temp1[K]=temp4
        temp4=temp4+temp2
     temp5=temp5+I
```

Optimize Loops – Loop Unrolling

- Modifying induction variable in each iteration can be expensive
- Can instead unroll loops and perform multiple iterations for each increment of the induction variable
- What are the advantages and disadvantages?

for (i = 0; i < N; i++) A[i] = ...

Unroll by factor of 4

Optimize Loops - Summary

- Low level optimization
 - Moving code around in a single loop
 - Examples: loop invariant code motion, strength reduction, loop unrolling
- High level optimization
 - Restructuring loops, often affects multiple loops
 - Examples: loop fusion, loop interchange, loop tiling